











Zoli 50 !

Combinatorial Optimization Day:  
Orientations, Matchings and Rigidity

Zoli will be 50 in a week !

Combinatorial Optimization Day:  
**Orientations, Matchings and Rigidity**

1. **Orientations and Connectivity**
2. Matchings, T-joins, Conservative weightings





Zoli will be 50 in a week !

Combinatorial Optimization Day:  
Orientations, Matchings and Rigidity

1. Orientations and Connectivity

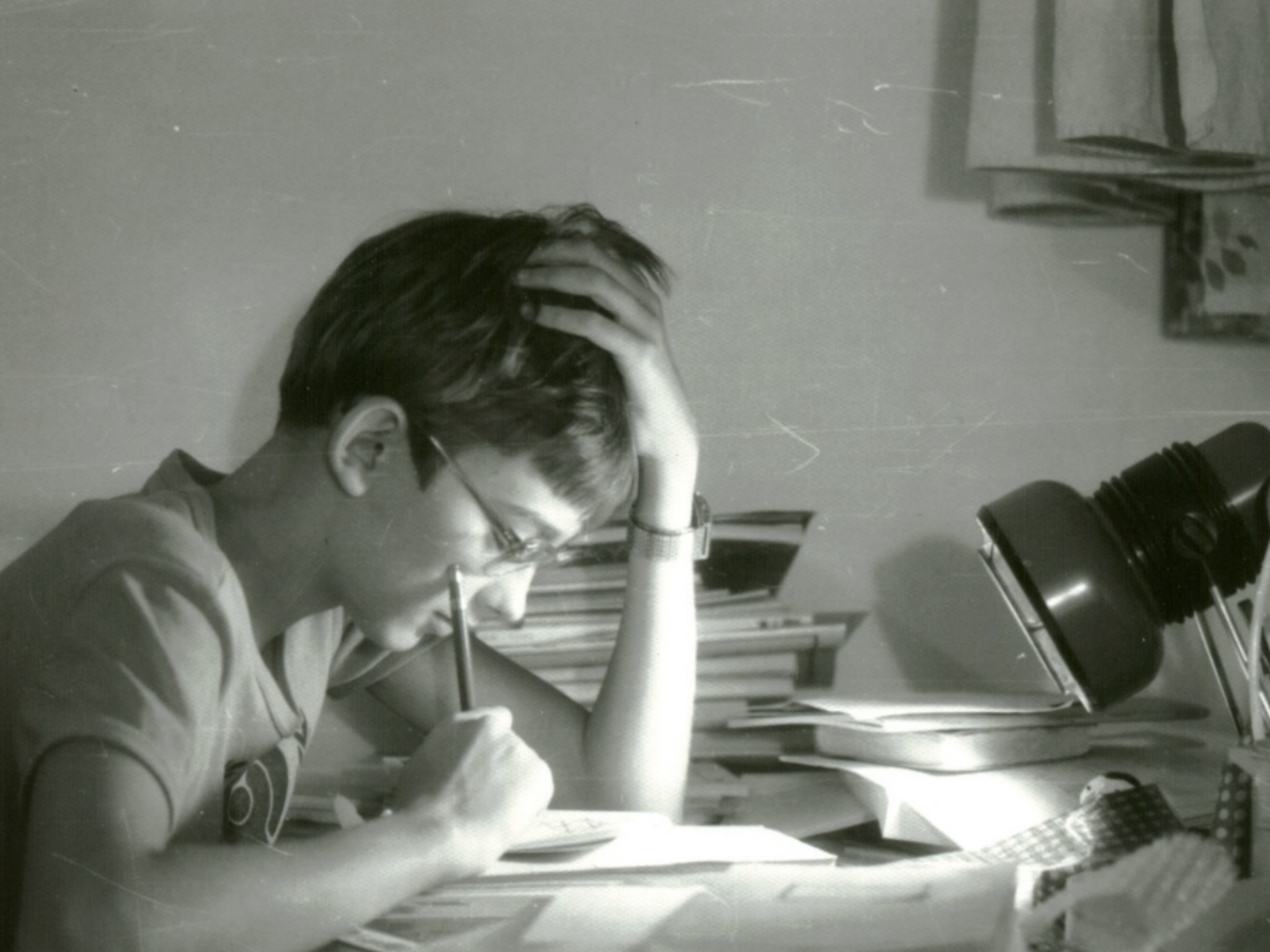
2. Matchings, T-joins, Conservative weightings

# Zoli and his work

## Scheduled part :

- I say some words about the **other main subject** of Zoli far from the preceding talks, & about his first steps **in maths**
- Jean Fonlupt speaks about his first steps **in France**
- Roland Grappe and Nguyen Viet Hăng speak about **Zoli's scientific descendance**
- Nadia Brauner tells us about **'Zoli and children'**

**Unscheduled part :** Please, take part at any time !





Zoli will be 50 in a week !

# Combinatorial Optimization Day: Orientations, **Matchings** and Rigidity

1. Orientations and Connectivity

2. **Matchings, T-joins, Conservative weightings**

# Theses

**Z. Szigeti**, *T-joins and T-cuts*, Master's Thesis, 1991, (en hongrois)

**Z. Szigeti**, *On conservative weightings of graphs*, Ph. D. Thesis, 1994, (en anglais)

**Z. Szigeti**, *Parity in graph theory*, Habilitation Thesis, 2000, (en français)

# Starting step

## two halves make a whole

### First Half

Z. Szigeti : On Seymour Graphs, Report No. 93803-OR, Research Institute for Discrete Mathematics, Bonn

Unpublished Manuscript

Seymour graphs: A rich class in which a certain minmax theorem holds, where  
**min contains** : postman, undir. min weight paths, ...  
**max contains** : routing

### Second Half

A. Ageev, A. Kostochka : A characterization of Seymour Graphs

Unpublished Manuscript

# A Characterization of Seymour Graphs \*

A. A. Ageev and A. V. Kostochka

Institute of Mathematics  
Universitetskii pr. 4, Novosibirsk 630090, Russia

## Abstract

Following Gerards [1] we say that a connected undirected graph  $G$  is a *Seymour graph* if the maximum number of edge disjoint T-cuts is equal to the cardinality of a minimum T-join for every even vertex subset  $T \subseteq V(G)$ . Several families of graphs have been shown to be subfamilies of Seymour graphs (Seymour [5][6], Gerards [1], Szígeti [7]). In this paper we prove a characterization of Seymour graphs which was conjectured by Sebő and implies the results mentioned above.

szuper@ludens.elte.hu,15:43 11/04/94 +...,

Date: Mon, 11 Apr 1994 15:43:43 +0200  
From: szuper@ludens.elte.hu  
To: andras.sebo@imag.fr

szia andras,

nagyon roviden vazolnam a dolgokat.

elozsoor is mindjart elkuldom neked a kosztocska-ageev paros cikkének új változatát. szerintem neked meg az eredeti teljesen rossz verzió van meg. ez teljesen jól olvasható és érthető. tulajdonképpen nagyon egyszerű dolgok történnek. lemma 1 a lényeg és az világos. (tulajdonképpen elege hasonlít a bizonyítás az én gerards tételre adott bizonyításomra, amit annak idején bennben elmeséltem neked.) szóval ez elég könnyen emészthető.

problema a tétel 1-gyel van. azt a feltételt, amelyik azt mondja, hogy (\*)  $\$G-C\$$  összefügg minden  $\$G-X_i\$$ -beli  $\$C\$$  komponensre, azt torolni kell. de mivel itt ez a feltétel nincs is felhasználva, ezért nincs is baj. ez a feltétel magához az egyes tétel bizonyításához kellett a kosztocskának.

azonban ahol neki szűkség volt erre a feltételre ott nekem sikerült megmutatnom, hogy e nélkül is megy.



# List of Publications

## ARTICLES DE REVUES

**A. Frank, Z. Szigeti**, *On packing T-cuts* ([pdf](#)), Journal of Combinatorial Theory, Series B, Vol. 61. No. 2. (1994) 263-271.

**A. Frank, Z. Szigeti**, *A Note on Packing Paths in Planar Graphs* ([pdf](#)), Math. Program. 70 (1995) 201-209

**Z. Szigeti**, *On a matroid defined by ear-decompositions of graphs* ([pdf](#)), Combinatorica 16 (2) (1996) 233-241

**A. Ageev, A. Kostochka, Z. Szigeti**, *A Characterization of Seymour Graphs* ([pdf](#)), Journal of Graph Theory, Vol. 24, No. 4, (1997) 357-364

**Z. Szigeti**, *The two ear theorem on matching covered graphs* ([pdf](#)), Journal of Combinatorial Theory, Series B, 74 (1998) 104-109

**Z. Szigeti**, *Hypergraph connectivity augmentation* ([pdf](#)), Math. Program. 84: (1999) 519-527

**J. Bang-Jensen, H. Gabow, T. Jordán, Z. Szigeti**, *Edge-connectivity augmentation with partition constraints* ([postscript](#)), SIAM Journal on Disc. Math. Vol. 12 No. 2 (1999) 160-207









Proposition

Def  $\vec{G}$  is a  $V=Z$   
is in the image of  $\vec{G}$   
 $m(s) = g \circ s \quad \forall s \in V$

Definition  $m(x) = \sum_{s \in X} m(s)$

Remark If  $m$  is in the image of  $\vec{G}$   
then  $m(x) = g \circ x$

Theorem of HAKIMI

Given  $G=(E)$  in  $V=Z$   
 $\exists$  an orientation (i.e. the  
direction of  $e \in E$ )  
 $\Leftrightarrow (a) \quad m(x) \geq 0 \quad \forall x \in X,$   
 $(b) \quad m(v) = |E|$

Pf Idea: bidirection  $E_i$

If  $E \neq \emptyset$   
Take  $s, t \in V$   
For  $e \in E$   $G = G - e + e$   
 $m(x) = m(x) + 1$   
(with  $e$  directed)

If  $G$  and  $a'$  satisfy the conditions  
by induction  $\exists$  an orientation  $\vec{G}$  of  $G$   
and then  $\vec{G} = \vec{G} + a'$  is an orientation of  $G$

which shows it is true that  $G$  and  $a'$  do not  
satisfy the conditions

$\Leftrightarrow \exists$  a hybrid set  $(m(x) = a(x))$  s.t.  
 $s \in X$  and  $t \notin X$

no one direction of intersecting hybrid sets on hybrid  
① intersection of intersecting hybrid sets is hybrid  
② the unique smallest hybrid set containing  $s$  contains  
all  $t \in V$

① If  $X$  and  $Y$  are hybrid and  $m \geq 0$   
then  $X \cap Y$  is hybrid

Pf  $m(x) = a(x) = a(x) + m(x)$   
 $\leq a(m) + m(x)$   
 $\leq a(x) + m(x)$   
 $= a(x)$

②  $(X, s) \cup (Y, t) \leq m(x)$



# List of Publications cont'd

**J. Cheriyan, A. Sebő, Z. Szigeti**, *Improving on the 1.5-approximation of a smallest 2-edge connected spanning subgraph* ([postscript](#)), SIAM Journal on Disc. Math. Vol. 14, No. 2, (2001) 170-180.

**A. Frank, T. Jordán, Z. Szigeti**, *An orientation theorem with parity conditions* ([pdf](#)), Discrete Applied Mathematics, 115 (2001) 37-47.

**Z. Szigeti**, *On generalizations of matching-covered graphs* ([pdf](#)), European Journal of Combinatorics, (2001) 22 865-877.

**Z. Szigeti**, *Perfect matchings versus odd cuts* ([postscript](#)), Combinatorica, 22 (4) (2002) 575-589.

**Z. Szigeti**, *The graphic matroid parity problem* ([pdf](#)), Journal of Combinatorial Theory / Series B, 88/2 (2003) 247-260.

**T. Jordán, Z. Szigeti**, *Detachments preserving local edge-connectivity of graphs* ([postscript](#)), SIAM Journal on Disc. Math. Vol 17, No. 1, (2003) 72-87.

# List of Publications cont'd

- Z. Szigeti**, *On a min-max theorem on bipartite graphs* ([pdf](#)), Discrete Mathematics, Special issue: 6th Int. Conf. on Graph Theory, eds.: J.-L. Fouquet, I. Rusu, Vol. 276/1-3, (2004) 353-361.
- Z. Király, Z. Szigeti**, *Simultaneous well-balanced orientations of graphs* ([pdf](#)), Journal of Combinatorial Theory, Series B, 96 (2006) 684-692.
- R. Grappe, Z. Szigeti**, *Covering symmetric semi-monotone functions* ([pdf](#)), Discrete Applied Mathematics 156 (2008) 138-144.
- Z. Szigeti**, *Edge-splittings preserving edge-connectivity of graphs* ([pdf](#)), Discrete Applied Mathematics, 156 (2008) 1011-1018.
- Z. Szigeti**, *Edge-connectivity augmentation of graphs over symmetric parity families* ([pdf](#)), Discrete Mathematics 308 (2008) 6527-6532.
- Z. Szigeti**, *On edge-connectivity augmentation of graphs and hypergraphs* ([pdf](#)), W. Cook, L. Lovász, J. Vygen (Editors): Research Trends in Combinatorial Optimization. Springer, Berlin 2009, 483-521.
- A. Bernáth, S. Iwata, T. Király, Z. Király, Z. Szigeti**, *Recent results on well-balanced orientations* ([pdf](#)), Discrete Optimization 5 (2008) 663-676.



# List of Publications cont'd

- A. Bernáth, S. Iwata, T. Király, Z. Király, Z. Szigeti**, *Recent results on well balanced orientations* ([pdf](#)), Discrete Optimization 5 (2008) 663-676.
- N. Jami, Z. Szigeti**, *Edge-connectivity of permutation hypergraphs* ([pdf](#)), Discrete Mathematics 312 (2012) 2536-2539.
- O. Durand de Gevigney, V. H. Nguyen, S. Klein, Z. Szigeti**, *Sandwich problems on orientations* ([pdf](#)), Journal of the Brazilian Computer Society: Volume 18, Issue 2 (2012), 85-93.
- Rautenbach, Z. Szigeti**, *Greedy colorings of words* ([pdf](#)), Discrete Applied Mathematics 160 (2012) 1872-1874.
- Bernáth, R. Grappe, Z. Szigeti**, *Augmenting the edge-connectivity of a hypergraph by adding a multipartite graph* ([pdf](#)), Journal of Graph Theory, 72/3 (2013) 291-312.
- Durand de Gevigney, V. H. Nguyen, Z. Szigeti**, *Matroid-based packing of arborescences* ([pdf](#)), SIAM Journal on Disc. Math. Vol. 27 No. 1 (2013) 567-574.
- Cheriyán, O. Durand de Gevigney, Z. Szigeti**, *Packing of rigid spanning subgraphs and spanning trees* ([pdf](#)), Journal of Combinatorial Theory, Series B, Volume 105, (2014) 17-25.

# List of Publications cont'd

- A. Bernáth, R. Grappe, Z. Szigeti**, *Covering symmetric crossing supermodular functions by partition constraints* ([pdf](#)), SIAM Journal on Disc. Math. 31/1 (2017) 335-382.
- Q. Fortier, Cs. Király, M. Léonard, Z. Szigeti, A. Talon**, *Old and new results on packing arborescences* ([pdf](#)), accepté dans Discrete Applied Mathematics
- O. Durand de Gevigney, Z. Szigeti**, *On  $(2k, k)$ -connected graphs* ([pdf](#)), soumis à Journal of Graph Theory (2017)
- Q. Fortier, Cs. Király, Z. Szigeti, S. Tanigawa**, *On packing spanning arborescences with matroid constraints*, ([pdf](#)), soumis à Combinatorica (Egres Technical Report No. TR-2016-18. Eötvös University) (2017)
- O. Durand de Gevigney, Z. Szigeti**, *On minimally 2- $T$ -connected graphs* ([pdf](#)), soumis à Discrete Applied Mathematics (Egres Technical Report No. TR-2017-05. Eötvös University) (2017)
- T. Matsuoka, Z. Szigeti**, *Polymatroid-Based Capacitated Packing of Branchings*, ([pdf](#)), soumis à Mathematical Programming (Technical Report No. METR 2017-15, University of Tokyo) (2017)

# Conferences

- Z. Szigeti**, *On Lovász's Cathedral Theorem* Proceedings of the Third Conference on Integer Programming and Combinatorial Optimization, eds.: G. Rinaldi, L.A. Wolsey, (1993) 413-423.
- A. Ageev, A. Kostochka, Z. Szigeti**, *A Characterization of Seymour Graphs*, Proceedings of the fourth Conference on Integer Programming and Combinatorial Optimization, eds.: E. Balas, J. Clausen, (1995) 364-372.
- J. Bang-Jensen, H. Gabow, T. Jordán, Z. Szigeti**, *Edge-connectivity augmentation with partition constraints*, Proc. 9th Annual ACM-SIAM Symp. on Disc. Alg. (1998) 306-315.
- J. Cheriyan, A. Sebő, Z. Szigeti**, *Improving on the 1.5-approximation of a smallest 2-edge connected spanning subgraph*, Proceedings of the sixth Conference on Integer Programming and Combinatorial Optimization, eds.: Bixby, Boyd, Rios-Mercado, (1998) 126-136.
- Z. Szigeti**, *On a min-max theorem of cacti*, Proceedings of the sixth Conference on Integer Programming and Combinatorial Optimization, eds.: Bixby, Boyd, Rios-Mercado, (1998) 84-95.
- Z. Szigeti**, *On optimal ear-decompositions of graphs*, Proc. 7th IPCO Conference, Graz, LNCS 1610, Springer, (1999) 415-428.
- A. Frank, T. Jordán, Z. Szigeti**, *An orientation theorem with parity conditions*, Proc. 7th IPCO Conference, Graz, LNCS 1610, Springer, (1999) 183-190.
- Z. Szigeti**, *On min-max results in matching theory*, 6th International Conference on Graph Theory, (Marseille, 2000), Electron. Notes Discrete Math., 5, Elsevier, Amsterdam, (2000) 291-294.

# Conferences cont'd

- Z. Szigeti**, *The nightmare of Mr Orient or orientation of graphs*, ROADEF 2003, extended abstract, Avignon, (2003) 212-213.
- Z. Szigeti**, *On the local splitting off theorem*, GRACO 2005, 2nd Brazilian Symposium on Graphs, Algorithms and Combinatorics, Electron. Notes Discrete Math., 19, Elsevier, (2005) 57-61.
- S. Iwata, T. Király, Z. Király, Z. Szigeti**, *On well-balanced orientations*, Proceedings of 4th Japanese Hungarian symposium on Discrete Mathematics and its Application, 2005
- R. Grappe, A. Bernáth, Z. Szigeti**, *Augmenting the edge-connectivity of a hypergraph by adding a multipartite graph*, Electron. Notes in Discrete Math. 34 (2009) 173-177.
- A. Bernáth, R. Grappe, Z. Szigeti**, *Partition constrained covering of symmetric crossing supermodular functions*, Proc. of Annual ACM-SIAM Symp. on Disc. Alg. (2010) 1512-1520.
- Z. Szigeti**, *On orientations of graphs*, Matemática Contemporânea, Vol 39 (2010) 179-188.
- A. Ageev, Y. Benchetrit, A. Sebő, Z. Szigeti**, *An excluded minor characterization of Seymour graphs*, Proc. 15th IPCO Conference, New York, LNCS 6655, Springer, (2011) 1-13.
- Cs. Király, Z. Szigeti**, *Reachability-based matroid-restricted packing of arborescences*, Proceedings of the 10th Hungarian-Japanese Symposium on Discrete Mathematics and Its Applications, 2017, Budapest, Hungary
- Q. Fortier, Cs. Király, Z. Szigeti, S. Tanigawa**, *On packing spanning arborescences with matroid constraints*, Electron. Notes Discrete Math., 61, (2017) 451-457.

## ARTICLES EN PREPARATION

**A. Ageev, Y. Benchetrit, A. Sebő, Z. Szigeti**, *An excluded minor characterization of Seymour graphs*.

## LIVRES EN PREPARATION

**Z. Szigeti, M. Preissmann**, *Optimisation Combinatoire et Graphes: Exercices et Solutions*, 300 pages, **Premiers deux chapitres** ([pdf](#))

## RAPPORTS DE RECHERCHE RECENTS

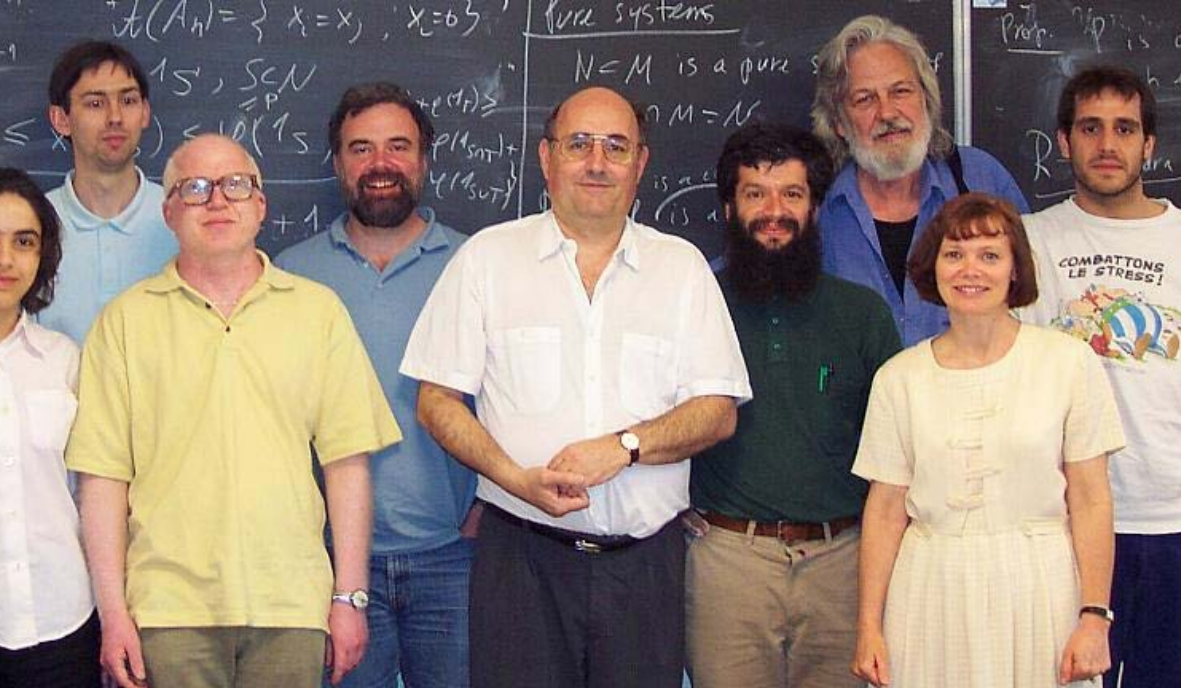
**Z. Szigeti, S. Tanigawa**, *An algorithm for the problem of minimum weight packing of arborescences with matroid constraints*, Technical Report No. METR 2017-14, University of Tokyo, (2017)

## MANUSCRITS

**Z. Szigeti**, *On Seymour Graphs*, Report No. 93803-OR, Research Institute for Discrete Mathematics, Universität Bonn, 1993

**D. Rautenbach, Z. Szigeti**, *Simultaneous large cuts*, Report No. 04937-OR, Research Institute for Discrete Mathematics, Universität Bonn, 2004,

**Q. Fortier, M. Léonard, Z. Szigeti, A. Talon**, *Old and new results on packing arborescences* ([pdf](#)), G-SCOP, Grenoble, 2016







*Many*

*Happy*

*Returns*

*Of the Day,*

*Zoli !*